

Freddy Bouchet, Cesare Nardini, and Tomás Tangarife **Non-equilibrium Statistical Mechanics of the Stochastic Navier-Stokes Equations and Geostrophic Turbulence**

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Alex Hansen, Per C. Hemmer, and Strutarshi Pradhan **The Fiber Bundle Model**

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Gerhard Nägele **Dynamics of Charged-Particles Dispersions**

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